



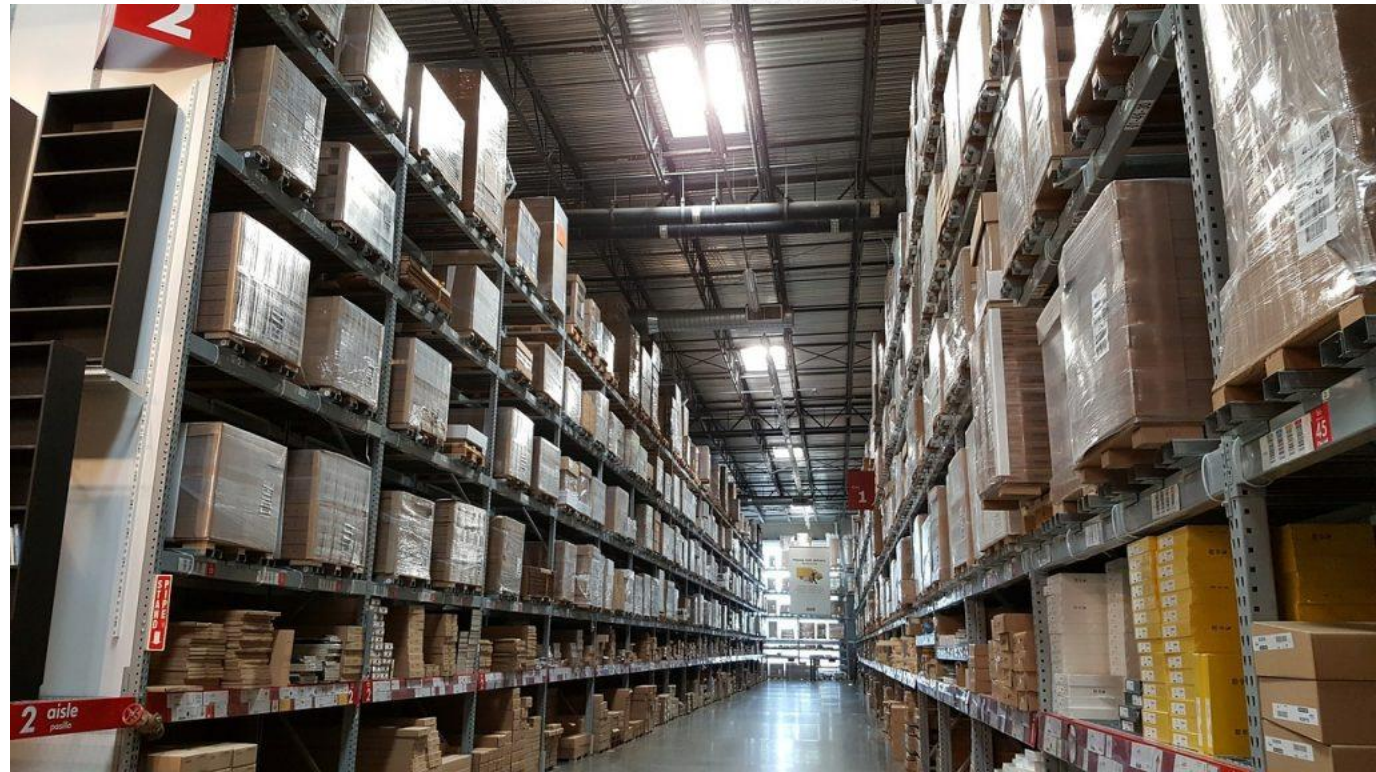
# Complementary- Similarity Learning using Quadruplet Network

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# E-commerce Recommender Systems



Nancy  
eCommerce Customer



Millions of items in eCommerce  
Catalog/ Warehouse



# Item Relationships

- Similarity/ Substitutes
  - Show similar items during exploration phase





# Item Relationships

- Complementary
  - Show after purchase add example e.g. if someone has purchased dress, additional suggestions like sandals, purse etc



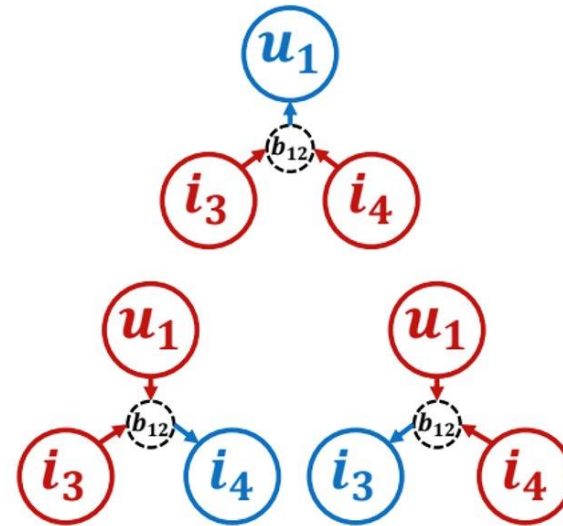


# Challenges

- "Functional" or "Stylistic"  
Complementarity is different than "bought together"
- Lack of ground truth for complementary items
- Cold-start items
- Differentiation between similar and complementary items

# Prior Work

- Triple2vec (Wan, CIKM 18)
  - Dual item embeddings
  - Maximize dot product between item pairs and user vectors
  - Challenges:
    - Solves co-purchasing more than "complementary"
    - Transitivity leads to similar items in recommendations
    - Does not handle cold-start items



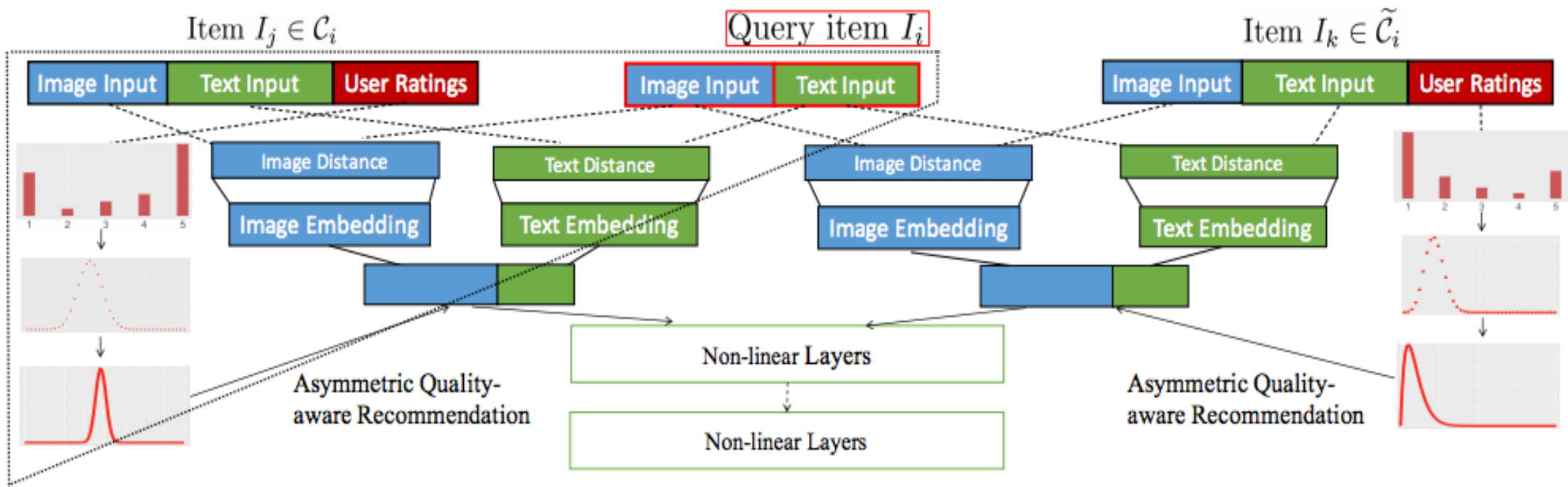
# Prior Work

- Neural Complementary Recommender (ENCORE) - (Zhang, RecSys 18)

$$P_{\text{comp}} = \sigma(d(a_f, c_f)) = \frac{1}{1 + e^{d(a_f, c_f) - \eta}} \quad [4]$$

Challenges:

- Transitivity



# Amazon Dataset

- Amazon Clothing, Shoes, and Jewelry data[2]
  - Category information and title
  - Complementary pairs: bought together by users from different categories
  - Similar pairs: items that lie in same category
  - Negative items: Randomly sample items which do not meet above criteria
  - Quads: anchor, complementary, similar, negative items
  - Train quads: 3.3M, Test quads:0.3M

<https://github.com/mansimane/quadnet-comp-sim>



# Amazon Dataset Attribute Availability

| Attribute   | Coverage |
|-------------|----------|
| Image       | 99.99    |
| Description | 5.68     |
| Title       | 99.95    |
| Price       | 38.29    |
| Brand       | 6.25     |

# Example Quadruplet

Anchor



Lee Dungarees Men's Big, Tall  
Carpenter Jean

Complementary



Key Apparel Men's Big-Tall  
Short Sleeve Heavyweight  
Pocket Tee Shirt

Similar



Wrangler Men's Rugged  
Wear Relaxed Straight Fit  
Jean

Negative



Black and White  
Herringbone Wool  
Suiting Extra Long Tie

# Motivation

- Why not just optimize for complementary items?

$$P_{\text{comp}} = \sigma \left( d(a_f, c_f) \right) = \frac{1}{1 + e^{d(a_f, c_f) - \eta}} \quad [4]$$



a

Wonder Nation Twist-Front Graphic T-Shirt



c

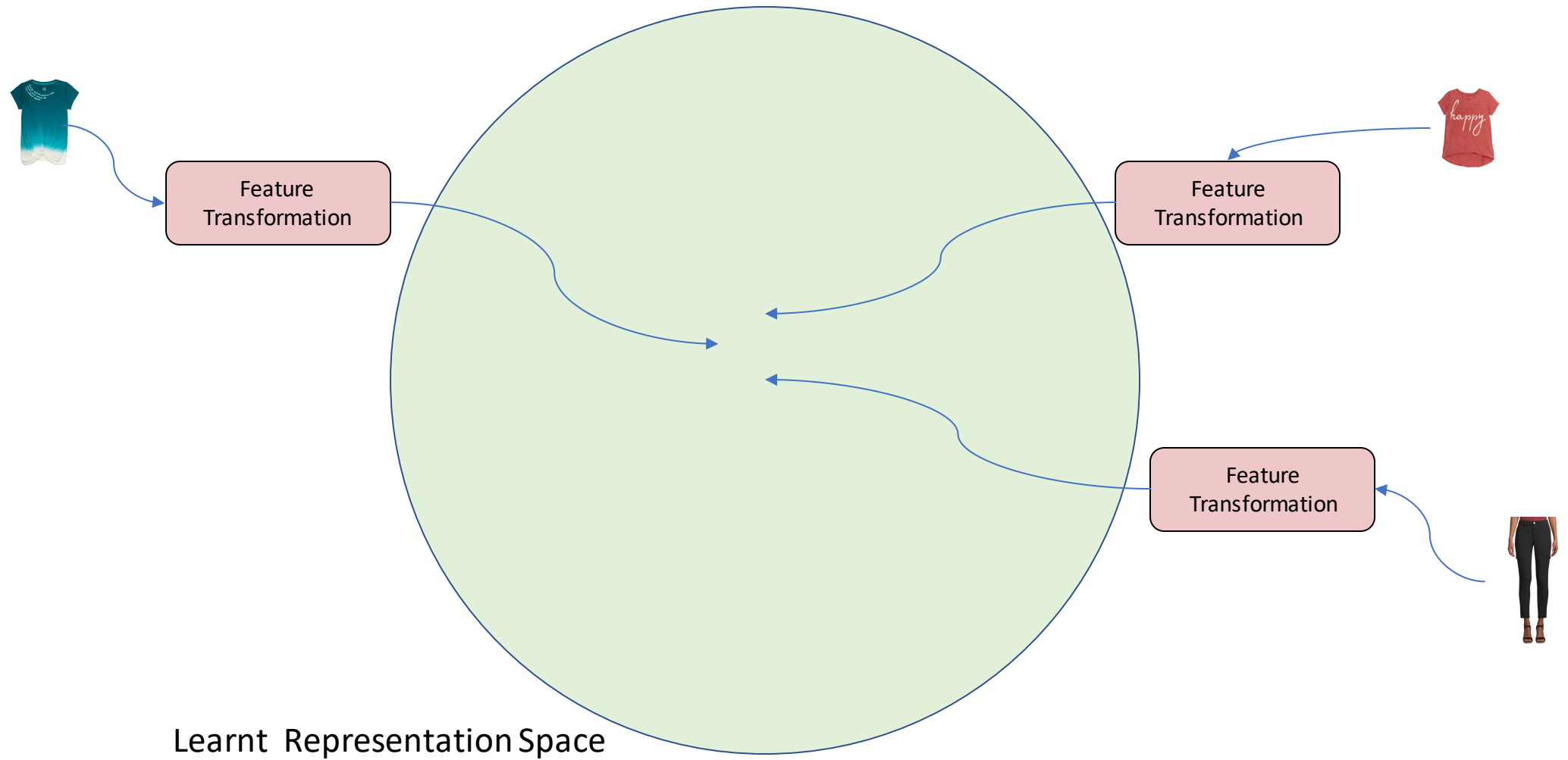
Women's Knit Skinny Cargo Pant



b

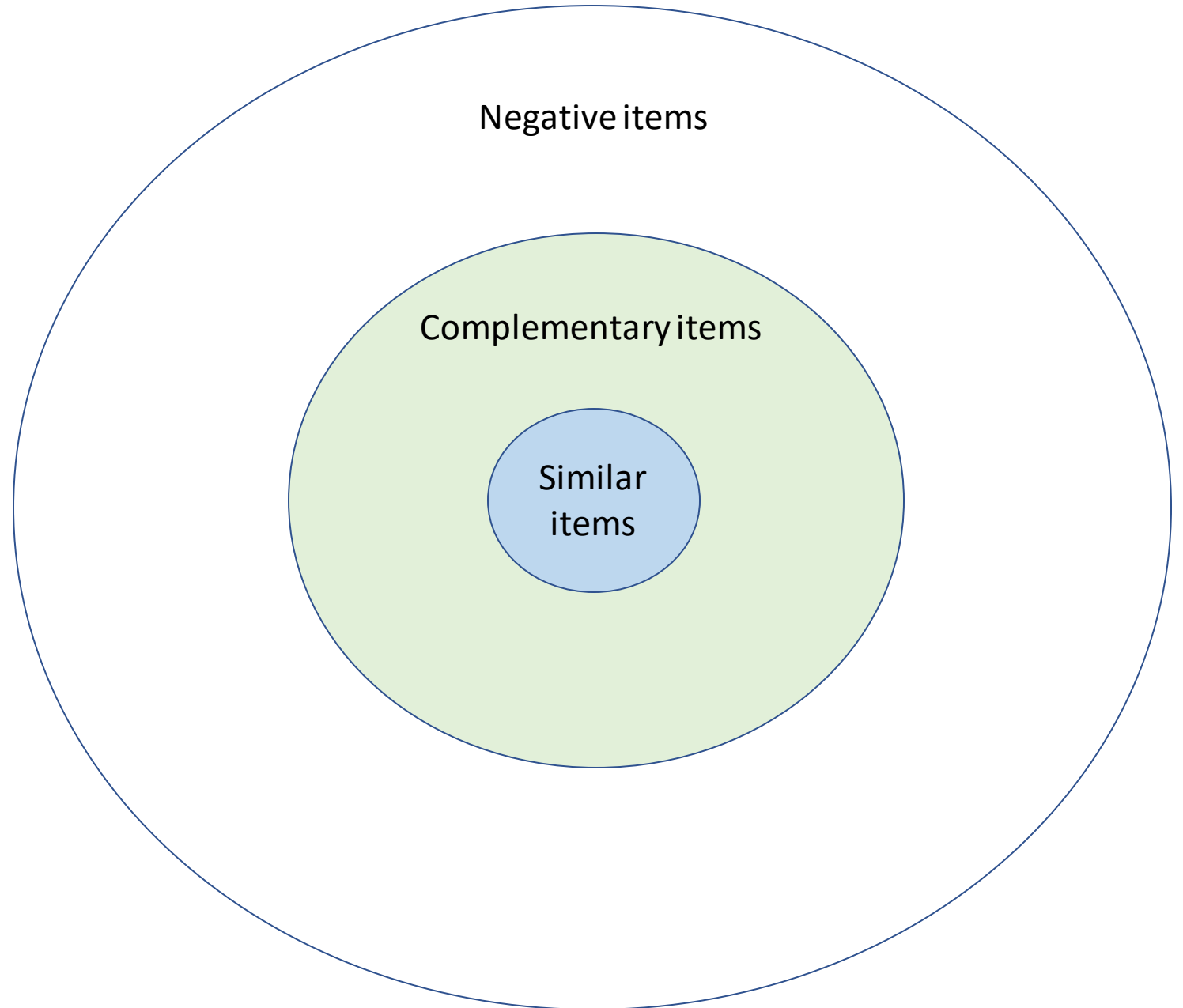
Wonder Nation Graphic Hi-Lo T-Shirt

# Motivation



# Goal

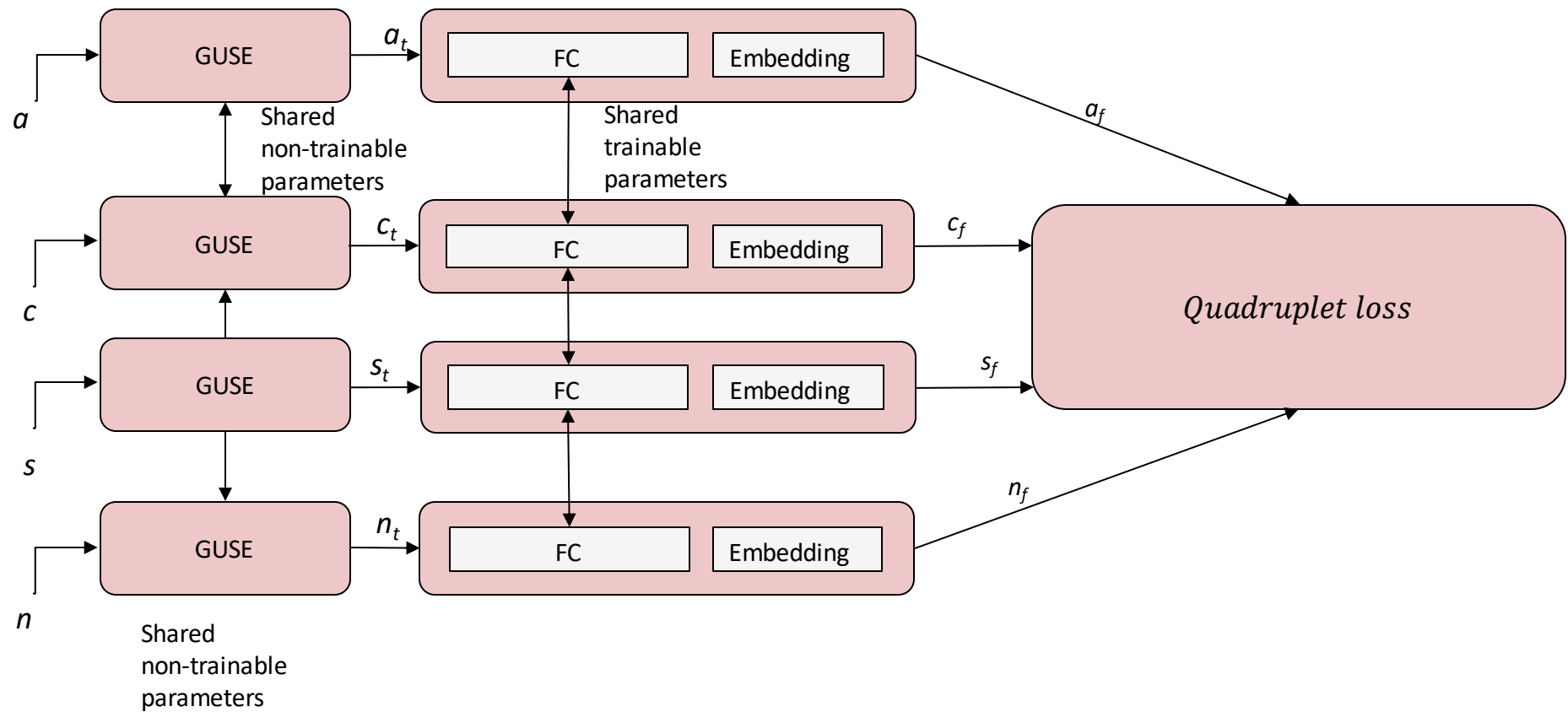
- Learn representation space which can differentiate between similar and complementary items



# Problem Formulation

- $a$ : Anchor item
- $c$ : Complementary item to anchor item
- $s$ : Similar item to anchor item
- $n$ : Negative item to anchor item
- $a'_f, c'_f, s'_f, n'_f$  : Normalized learnt feature representation for  $a, c, s, n$

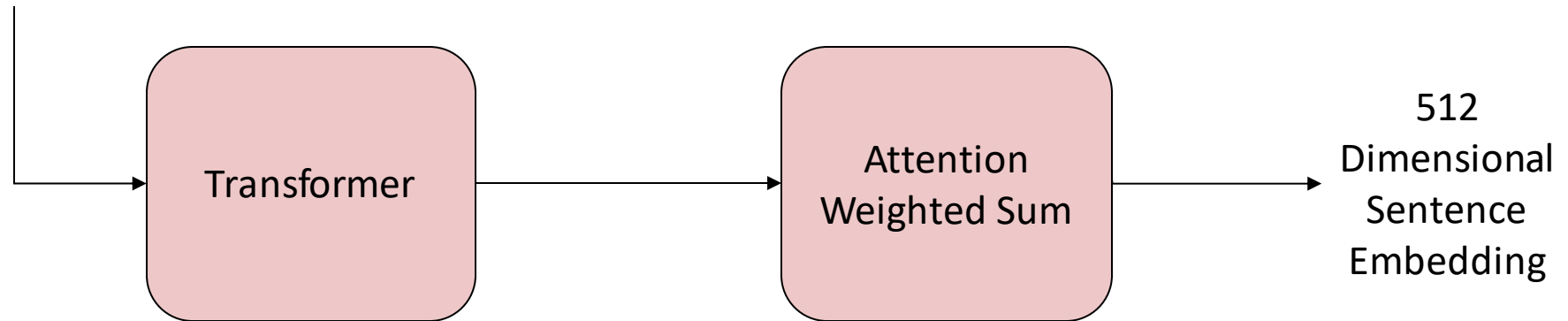
# Network Architecture



# Feature Representation

- Universal Sentence Encoder [1]

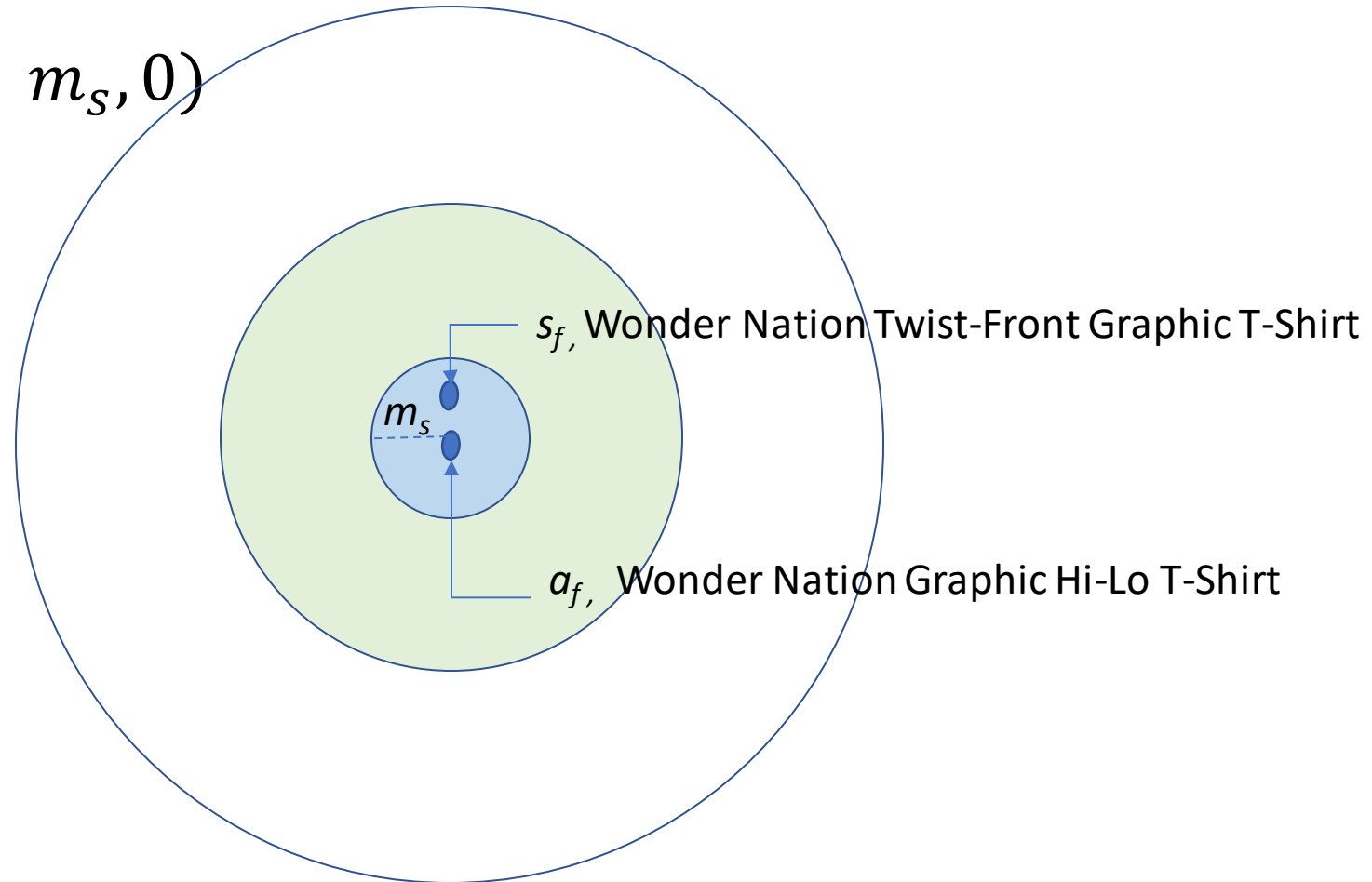
Wonder Nation Twist-Front Graphic T-Shirt





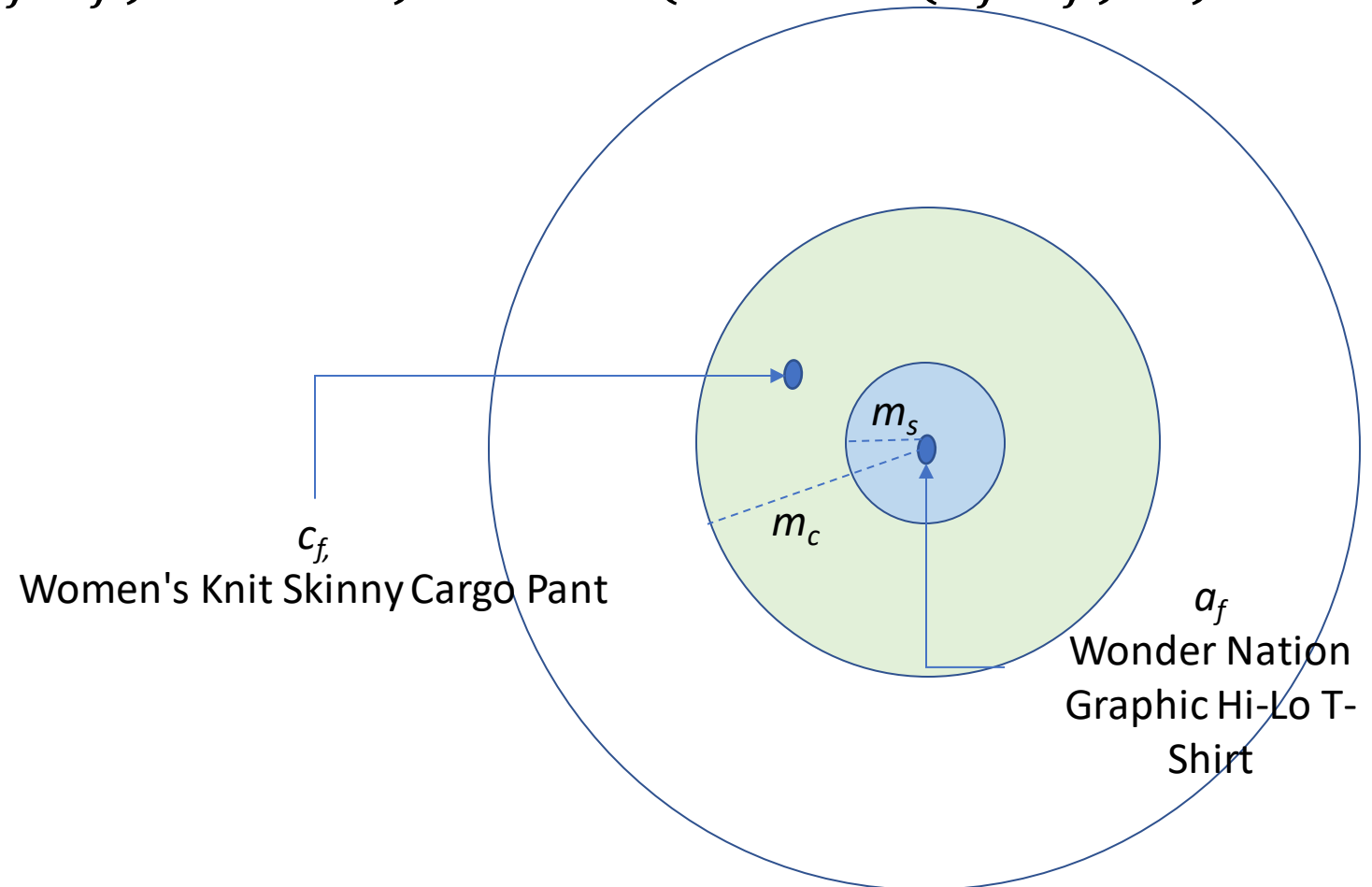
# Similarity Loss

- $L_{sim} = \max(d(a'_f - s'_f) - m_s, 0)$



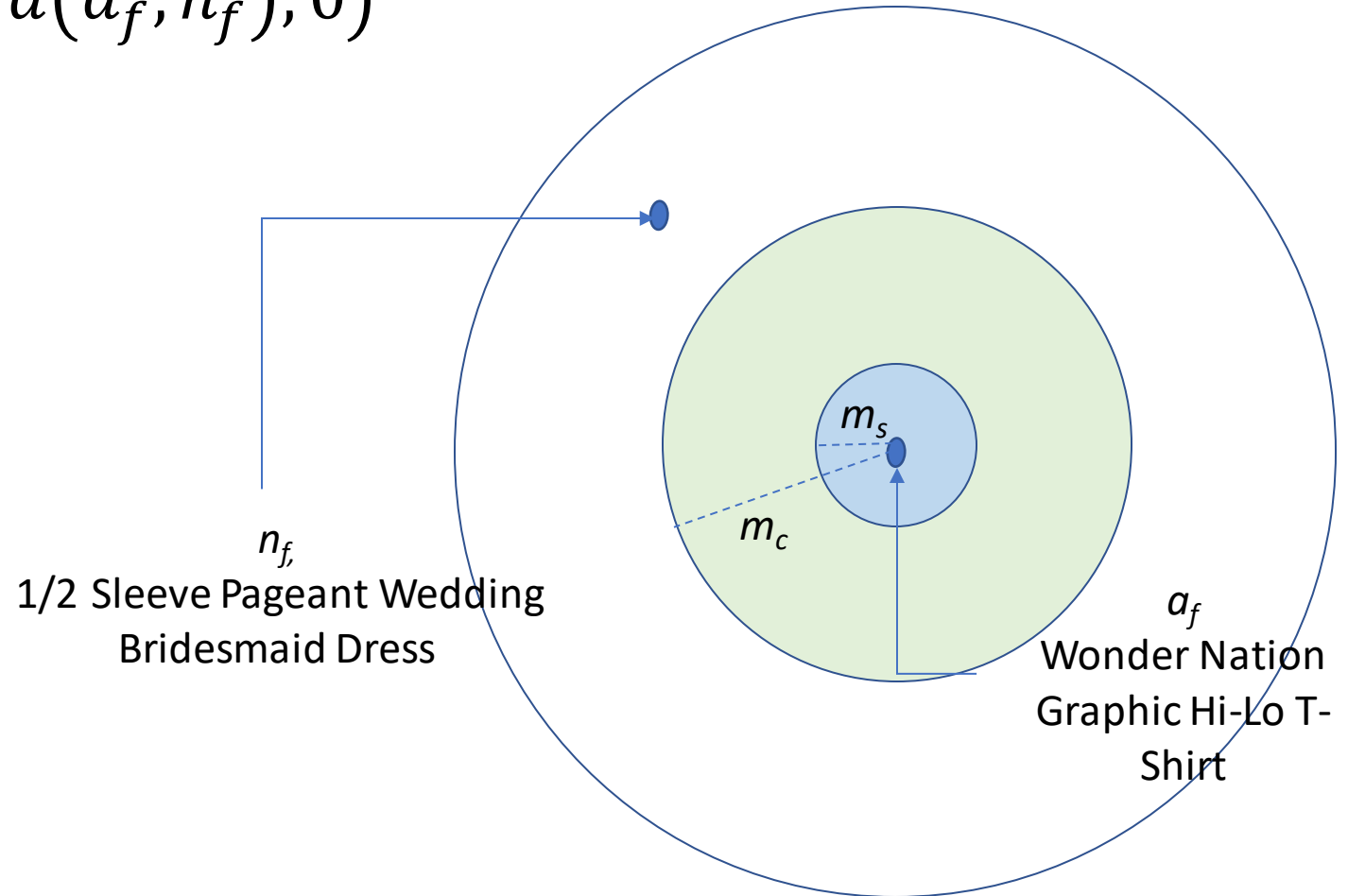
# Complementary Loss

- $L_{comp} = \max(d(a'_f, c'_f) - m_c, 0) + \max(m_s - d(a'_f, c'_f), 0)$



# Negative Loss

- $L_{neg} = \max(m_n - d(a'_f, n'_f), 0)$

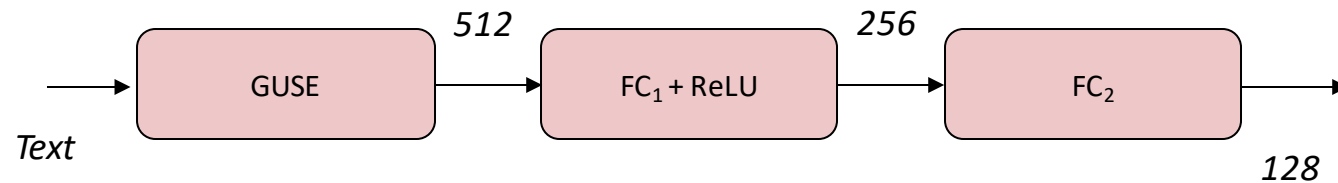


# Quadruplet Loss

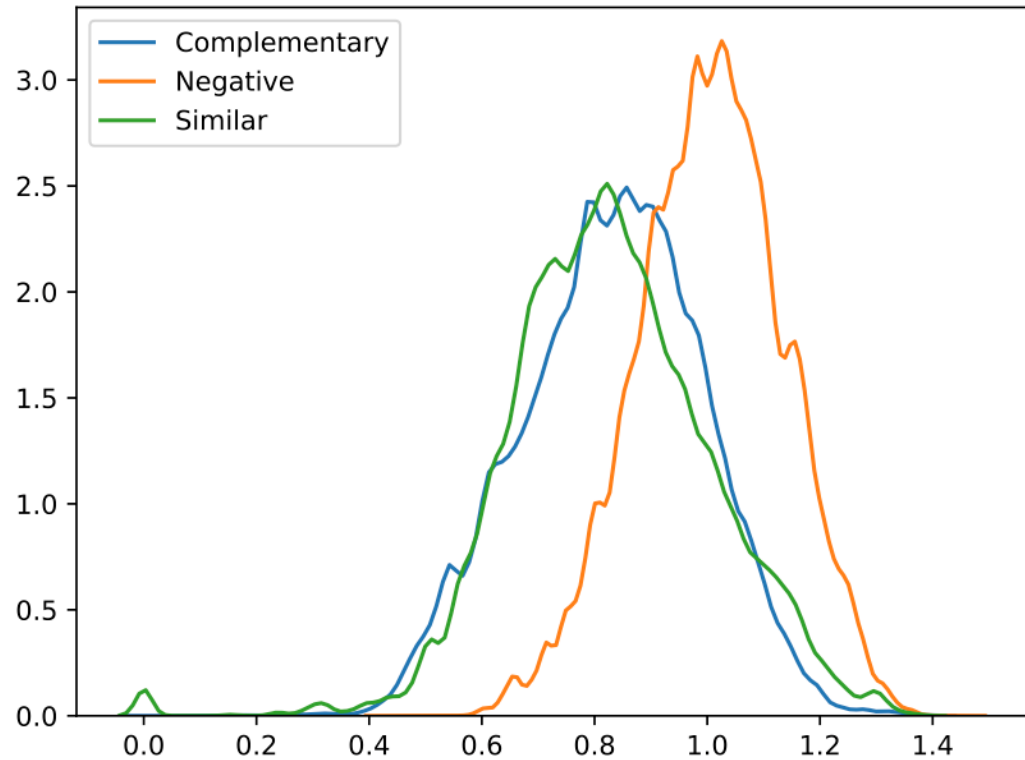
- $L_{sim} = \max(d(a'_f - s'_f) - m_s, 0)$
- $L_{comp} = \max(d(a'_f, c'_f) - m_c, 0) + \max(m_s - d(a'_f, c'_f), 0)$
- $L_{neg} = \max(m_n - d(a'_f, n'_f), 0)$
  
- $L_{quad} = L_{sim} + L_{comp} + L_{neg} + \lambda L_{l2}$

# Hyperparameters

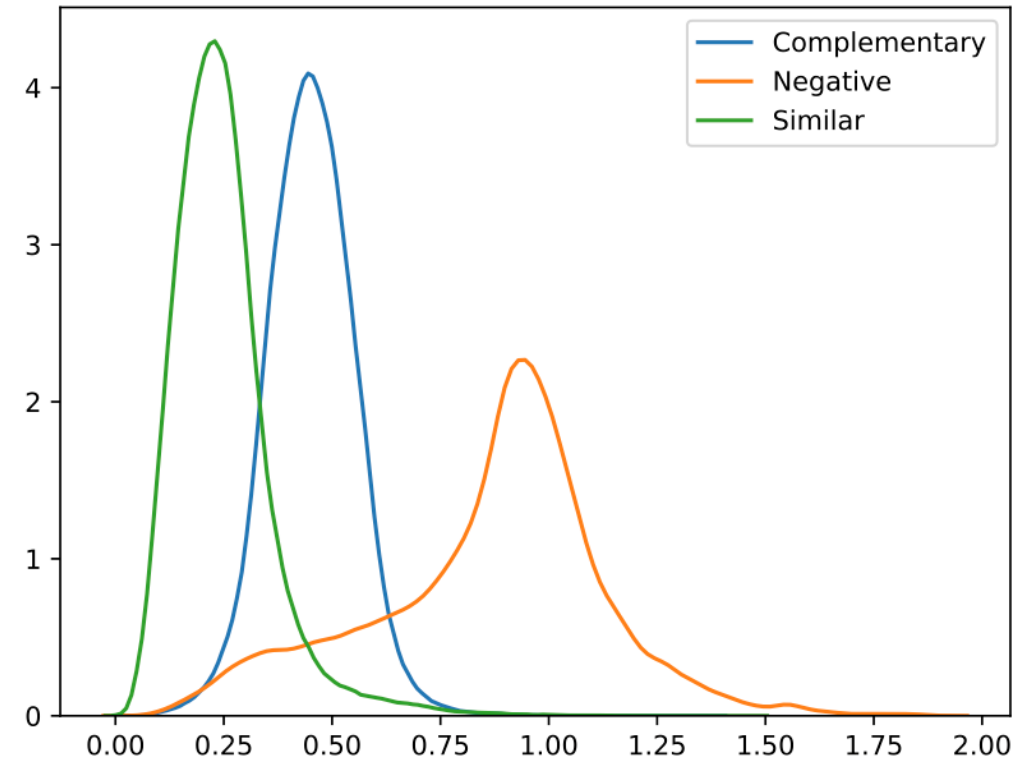
- Input feature dimension: 512
- Epochs: 50
- Weight Initialization: Xavier
- Learning rate: 0.001
- $m_s$  : 0.1
- $m_n$  : 0.4
- $m_c$  : 0.8
- Mapping function:



# Experiments - Distance Distribution



Before Training



After Training

# Experiments - Distance Distribution

|                            | Similar |         | Complementary |         | Negative |         |
|----------------------------|---------|---------|---------------|---------|----------|---------|
|                            | Mean    | Std Dev | Mean          | Std Dev | Mean     | Std Dev |
| Train Data Before training | 0.82119 | 0.17611 | 0.81975       | 0.15910 | 0.99804  | 0.13286 |
| Test Data Before training  | 0.82752 | 0.17853 | 0.83086       | 0.15937 | 1.0037   | 0.12949 |
| Train Data After training  | 0.24069 | 0.11226 | 0.45845       | 0.11485 | 0.86774  | 0.27724 |
| Test Data After training   | 0.24772 | 0.11485 | 0.45181       | 0.09963 | 0.86023  | 0.27182 |

## Experiments Accuracy

| Method                     | Ranking Acc  | Complementary Acc | Similarity Acc |
|----------------------------|--------------|-------------------|----------------|
| Universal Sentence Encoder | 37.68        | -                 | -              |
| Veit et al. [2]            | 14.92        | 91.05             | 56.45          |
| Quadruplet Network         | <b>67.15</b> | 86.92             | <b>68</b>      |

- Ranking accuracy is calculated as:  $d_s < d_c < d_n$
- Complementary Accuracy:  $\text{margin}_s < d_c < \text{margin}_c$
- Similarity Accuracy:  $d_s < \text{margin}_s$



# Inference (offline or RT)

- Use Approximate Nearest Neighbor (ANN) indices (FAISS, annoy, nmslib) to perform top-k embedding retrieval
- Divide all items into  $C$  disjoint groups (via taxonomy or clustering on embeddings)
- Create a set of ANN indices:
  - 1 global item index
  - 1 cluster centroid index
  - $C$  separate cluster indices (of item embeddings associated with that cluster)

# Inference (offline or RT)

- Given query item, obtain query embedding from quadruplet network
- Given a query embedding:
  - Top K similar items:
    - Nearest neighbor (NN) query on the item index
  - Top K complementary items:
    - Goal: Find K closest items whose distance is in range  $[ \text{margin}_c, \text{margin}_s )$
    - 1 ) NN query on the cluster index, consider the centroids in range
    - 2) For each in-range cluster, find the top K closest items. Merge the sets and retain the top K in range  $[ \text{margin}_c, \text{margin}_s )$

# Future Work

- Modelling asymmetry between relationships
- Large scale experiments on the Amazon dataset (and others) with more evaluation metrics
- Clustering analysis on learnt embedding space

# References

1. Cer, Daniel, et al. "Universal sentence encoder" *arXiv preprint arXiv:1803.11175* (2018).
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Thank You

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